INTRODUCTION

Monitoring meteorological and oceanographic conditions is crucial to improve numerical weather prediction models (Centurioni et al., 2016) and to manage and assess the safety of coastal and offshore operations. Wave measurements represent a key feature of environmental monitoring programs in several countries around the world. In-situ wave measurements are important for the calibration and validation of advanced wave models that support coastal warning systems, as well as for the design, construction and operational planning of ports and harbors. Since the early 1960s commercial surface-following wave measuring devices have been deployed to collect in-situ measurements of ocean and coastal surface waves.

In recent years, the Global Positioning System (GPS) technology has been introduced in wave buoys as an alternative to motion package based instruments, which utilize gimbaled or strapped down accelerometers along with a compass to measure the pitch, heave and roll of the buoy (Krogstad et al., 1997; Krogstad et al., 1999; Herbers et al., 2012). Modern GPS receivers have improved the performance of GPS-based wave buoys, which have become a robust alternative to traditional well-established motion-sensor based sensors such as the Datawell Directional Waverider MKII (DWR-2) and newer generation DWR-3 (De Vries et al., 2003; Jeans et al., 2003; Colbert, 2010; Herbers et al., 2012). The GPS technology is also used to obtain the geo-location of Lagrangian Surface Velocity program (SVP) drifters used to measure the world ocean surface circulation (Niiler, 2001; Maximenko et al., 2013, Centurioni, 2016) and for other heavily instrumented drifting buoys designed for nearshore or surf-zone applications (e.g. Postacchini et al., 2016).

The GPS measurement principle is based on the Doppler shift of the satellite signal frequency and provides the three velocity components of the buoy and thus of the sea surface, under the assumption that the buoy is a good water surface follower. The advantages of this technology are both practical and economical (Krogstad et al., 1999). The GPS receiver is very cost-effective and can be implemented in small, light-weight buoys, which can be deployed from small boats. The contained dimensions of Directional Wave Spectra Drifter (DWSM hereafter) described in this paper result in a better response...
of the buoy to high wave frequency, thus extending the observation range. Furthermore, since there are no moving parts, fluxgate compasses and the velocity of the water surface is measured in a fixed reference frame from external GPS signals, the DWSD does not need calibration. If the DSWD is deployed as a fixed installation, particular care is needed in the design of the mooring line or the buoy and the GPS antenna will submerge, thus stopping the velocity data acquisition and introducing gaps in the velocity time series. The submerging force can be reduced by reducing the mooring line angle with conventional mooring design solutions utilizing a secondary float or natural rubber bungee. A possible alternative to a vertical mooring could be a horizontal mooring to a vessel or float. Such a configuration mitigates the problem of the buoy submersion while preventing the buoy from getting adrift (de Vries, 2007). Other potential disadvantages of this innovative system are the possible errors and biases of the GPS measurements, classified as satellite-dependent errors, signal propagation-dependent errors and receiver-dependent errors (Joodaki et al., 2013).

In this work, a GPS-based DWSD, recently developed by the Lagrangian Drifter Laboratory (LDL) at Scripps Institution of Oceanography (SIO), is evaluated. In the next two sections we describe the technical characteristics of the device and the data processing methodology, followed by the details of the test campaign, that was designed to compare the performance of the DWSD deployed in the proximity of a bottom-mounted Teledyne-RD Instruments Acoustic Doppler Current Profiler (ADCP) in the Gulf of Naples, Italy. The results, conclusions and future applications are discussed in the last two sections.

THE DWSD

Stemming from the drifter design adopted by the Global Drifter Program (GDP) (Niiler, 2001; Maximenko et al., 2013, Centurioni et al. 2016), the DWSD (Fig. 1), consists of a sphere with a diameter of 0.39 m, 12 Kg weight and replaceable alkaline or lithium batteries. The DWSD GPS sensor measures the vertical (w), zonal (east-west, u) and meridional (south-north, v) velocity components of the buoy. Times series of u(t), v(t) and w(t) are sampled for ≈17 min at 2 Hz and are split into 4 overlapping segments of 256 s that are subsequently averaged. The power spectral density, co-spectra and quadrature-spectra parameters are derived with the Fourier transforms of the correlation functions of each pair of the velocity time-series, giving the First-5 independent Fourier coefficients (a_0, a_1, a_2, b_1, b_2) and thus the wave spectra for each hourly (and optionally, half-hourly) sea state. For each measured sea state, the three velocity components, the computed first 5 Fourier coefficients and the directional wave parameters can be stored onboard into an optional data logger while platform information (timestamp latitude, longitude, battery voltage, internal pressure, temperature and humidity) at start of data collection, directional wave parameters and optionally, the first 5 Fourier coefficients from 0.031Hz-0.496Hz with 1/256Hz bandwidth are transmitted to shore in real-time through the Iridium satellite system. Using two-way Iridium communication, the GPS-based wave buoy can be programmed while deployed to modify the duration of sampling in multiples of 256 seconds, deployment depth, as well as toggle first 5 reporting to shore for power consumption and telemetry cost savings. All of the transmitted wave data, as well as platform status are accessible in real time on a dedicated website.

Figure 1. (a) The DWSD and (b) its internal layout.
DATA PROCESSING

Directional and non-directional wave spectra

The directional variance spectra $S(f, \theta)$ of each sea state measured by the DWSD is estimated using the truncated Fourier series up to the second-order terms, expressed as (Lounguet-Higgins et al., 1963; Mitsuyasu et al., 1975; Long, 1980):

$$S(f, \theta) = \frac{a_0}{2\pi} \left[1 + 2 \sum_{m=1}^{2} [a_m \cos(m\theta) + b_m \sin(m\theta)]\right]$$  \hspace{1cm} (1)

The first five coefficients $(a_0, a_1, a_2, b_1, b_2)$ of the truncated Fourier series in Eq. 1 are obtained from the complex cross-spectral and quadrature spectra $C_{11}$, $C_{22}$, $C_{33}$, $C_{23}$, $Q_{12}$, $Q_{13}$ using the relations for single-point measuring devices recording the three velocities components (Benoit et al., 1997):

$$a_0(f) = C_{11} \left(\frac{1}{2\pi f} \frac{\sinh(kd)}{\sinh(k(d + z))}\right)^2$$ \hspace{1cm} (2)

$$a_1(f) = \frac{Q_{12}}{\sqrt{C_{11}(C_{22} + C_{33})}}$$ \hspace{1cm} (3)

$$b_1(f) = \frac{Q_{13}}{\sqrt{C_{11}(C_{22} + C_{33})}}$$ \hspace{1cm} (4)

$$a_2(f) = \frac{C_{22} - C_{33}}{C_{22} + C_{33}}$$ \hspace{1cm} (5)

$$b_2(f) = \frac{2 \cdot C_{23}}{C_{22} + C_{33}}$$ \hspace{1cm} (6)

The wavenumber $k$, defined as $2\pi/\lambda$, where $\lambda$ is the wavelength of the harmonic wave, is related to the frequency $f$ by the dispersion relation of the linear wave theory:

$$(2\pi f)^2 = (gk) \tanh(kd)$$ \hspace{1cm} (7)

In Eq. 7, $g$ is the acceleration due to gravity and $d$ is the water depth.

The shallow water correction applied in the DWSD onboard processing software is then (Herbers et al., 2012):

$$C_{11} = \tanh^2(kd) [C_{22} + C_{33}]$$ \hspace{1cm} (8)

Wave Parameters

The directional wave spectra $S(f, \theta)$ in Eq. 1 can be also be written as (Huang et al., 1998):

$$S(f, \theta) = E(f) \cdot D(f, \theta)$$ \hspace{1cm} (9)

In Eq. 9, $E(f)$ is the non-directional variance spectrum estimated from the sea-surface elevation,

$$E(f) = \int_{0}^{2\pi} S(f, \theta) d\theta = C_{11}(f)$$ \hspace{1cm} (10)

and $D(f, \theta)$ is the Directional Spreading Function (DSF), which represents the directional distribution of the variance at each frequency. In this paper, $D(f, \theta)$ is computed as (Steele et al., 1992):

$$D(f, \theta) = \frac{1}{\pi} \left[\frac{1}{2} + r_1 \cos[\theta - \theta_1] + r_1 \cos[2(\theta - \theta_2)]\right]$$ \hspace{1cm} (11)

where:

$$r_1 = \frac{1}{a_0} \left(a_1^2 + b_1^2\right)^{0.5}$$ \hspace{1cm} (12)

$$r_2 = \frac{1}{a_0} \left(a_2^2 + b_2^2\right)^{0.5}$$ \hspace{1cm} (13)
\[ \theta_1 = \tan^{-1}\left(\frac{b_1}{a_1}\right) \]  
(14)

\[ \theta_2 = \frac{1}{2}\tan^{-1}\left(\frac{b_2}{a_2}\right) \]  
(15)

\( \theta_1 \) and \( \theta_2 \) are called, respectively, the mean wave direction and principal wave direction. The two solutions of Eq. 15 for \( \theta_2 \) differ by \( \pi \), and the value closer to \( \theta_1 \) is used in this work. Both \( \theta_1 \) and \( \theta_2 \) do not depend on the vertical GPS velocity, which may be noisier than the horizontal velocity (Colbert, 2010).

The wave parameters are calculated from the directional and non-directional wave spectra. The significant wave height, \( H_s \), is obtained from the wave elevation variance \( m_0 \):

\[ H_s = 4.004\sqrt{m_0} \]  
(16)

where \( m_0 \) is the zeroth-order moment of the non-directional wave spectrum \( E(f) \), defined by:

\[ m_0 = \pi \Delta f \sum_{n=1}^{N_b} a_{0,n} \quad n = 1, 2, ..., N_b \]  
(17)

where \( \Delta f = 0.0039 \text{ Hz} \) is the frequency bandwidth of the DWSD and \( N_b \) is the number of bands in the frequency range 0.039 Hz < \( f < 0.49 \text{ Hz} \).

The mean wave period is defined as:

\[ T_a = \frac{m_0}{m_1} \]  
(18)

where \( m_1 \) is the first-order moment defined as:

\[ m_1 = \pi \Delta f \sum_{n=1}^{N_n} f_n \cdot a_{0,n} \]  
(19)

The peak period, \( T_p \), is defined by the reciprocal of the center frequency of the non-directional spectral band with the maximum spectral density, \( f_p \):

\[ T_p = \frac{1}{f_p} \]  
(20)

Finally, the wave peak direction, \( D_p \), is defined as the wave direction (Eq. 14) at the maximum of directional wave spectra \( S(f, \theta) \):

\[ D_p = \theta_1(f_p) = \tan^{-1}\left(\frac{b_1}{a_1}\right)_{f=f_p} \]  
(21)

In this work, the peak direction is converted according to the nautical convention, i.e. as the incoming wave direction, measured clockwise from the north and time is expressed in Coordinated Universal Time (UTC). The comparison of the wave parameters is performed for wind waves only since they contained the largest energy (Earle, 1984; Voorrips et al., 1997; Wang and Hwang, 2001; Gilhousen and Hervey, 2001; Violante-Carvalho et al., 2002; Portilla et al., 2009; Portilla et al., 2015), using a separation frequency \( f_s = 0.11 \text{ Hz} \). Fig. 2 shows an example the non-directional variance spectrum \( E(f) \) with the separation frequency marked between two distinct peaks. In other words, in the following, we restrict the analysis to the 0.11 Hz - 0.49 Hz frequency range.
Figure 2. Example of the non-directional spectral variance density $E(f)$ showing the separation frequency ($f_s$) used to partition the wave spectrum between wind and swell.

EXPERIMENTAL TEST CAMPAIGN

The DWSD was deployed for approximately 6 days, from May 12 to May 18, 2016 at 40°49.668’ N and 14° 13.984’ E and was co-located with an ADCP at a water depth of 17.5 m (Fig. 3) and within 30 m a distance. The bottom-mounted, upward-looking, four beams, 600 kHz, ADCP by RDI is part of a wave measurement facility of the Stazione Zoologica “Anton Dohrn”, Naples. The ADCP directional wave measurement principle (Pinkel and Smith, 1987; Krogstad et al., 1988; Smith, 1989; Terray et al., 1999; Strong et al., 2000) is based on computing the water velocity from the Doppler shift of the backscattered acoustic pulses along the four inclined beams. The non-directional wave spectra are computed in Earth’s coordinates from the water velocity data. The ADCP also measures the non-directional spectra through echo ranging (surface track) and bottom pressure with a pressure transducer, providing alternative measurements of the surface elevation and of the water depth. It should be noted that the methodology used by the ADCP software to compute the directional wave parameters different from the one used by the DWSD. The ADCP software uses the Maximum Likelihood Method (MLM, e.g. Terray et al., 1999) that computes the spectra from each velocity time series at each sensor, from which the wave phase information is subsequently obtained.

The non-directional wave parameters from the ADCP were computed from both the velocity and surface tracking spectra using a frequency bandwidth of 0.0078 Hz and using the same separation frequency $f_s = 0.11$ Hz use for the DWSD analysis. The deployment configuration settings of the ADCP are given in Table 1 and the parameters used for processing and extracting the wave parameters are given in Table 2. As a self-consistency check for the ADCP, the wave parameters for which $T_p$ computed from the two spectra differed by more than 1s, were discarded.
Figure 3. (a) Location of the field site of the test campaign at the Gulf of Naples (Italy) and (b) detail of the test site. (c) the DWSD is the yellow buoy located next to the measurement station where the ADCP was bottom-mounted.

Table 1: Deployment configuration setting of the ADCP

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Setting</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water depth</td>
<td>17.7 m</td>
</tr>
<tr>
<td>Sampling interval</td>
<td>3600 s</td>
</tr>
<tr>
<td>ADCP altitude above bottom</td>
<td>0.5 m</td>
</tr>
<tr>
<td>Number of samples per burst (at 2 Hz)</td>
<td>2100</td>
</tr>
<tr>
<td>Size of the depth cell</td>
<td>0.5 m</td>
</tr>
<tr>
<td>Bins used for directional spectrum</td>
<td>1,13,27,28,29</td>
</tr>
<tr>
<td>Bins used for height spectrum</td>
<td>1,13,27,28,29</td>
</tr>
<tr>
<td>Maximum cutoff frequency</td>
<td>0.95 Hz</td>
</tr>
<tr>
<td>Minimum Included wave period</td>
<td>1.05 s</td>
</tr>
<tr>
<td>Frequency range</td>
<td>0 to 1.0 Hz</td>
</tr>
</tbody>
</table>
Table 2: Parameters used for the ADCP wave processing

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Frequency bandwidth</td>
<td>0.0078 Hz</td>
</tr>
<tr>
<td>Maximum upper cutoff frequency</td>
<td>0.49 Hz</td>
</tr>
<tr>
<td>Minimum lower cutoff</td>
<td>0.11 Hz</td>
</tr>
<tr>
<td>Number of direction frequency bands</td>
<td>128 bands</td>
</tr>
</tbody>
</table>

RESULTS

During the observation period, the sea-state reached peaks of significant wave height of 0.8-0.9 m on May 14, 2016 (Fig. 4). To quantify the difference of the directional and non-directional wave properties obtained with the two instruments, statistical indicators such as the bias and root mean square error (RMSE) were used:

\[
Bias = \frac{1}{N} \sum_{i=1}^{N} (y_i - x_i)
\]

\[
RMSE = \sqrt{\frac{1}{N-1} \sum_{i=1}^{N} (y_i - x_i)^2}
\]

where \(y_i\) and \(x_i\) indicate the waves parameters obtained from the two sensors at the i-th hourly sea state, and N is the total number of sea-states under evaluation. The data from which the bias and the RMSE were computed are shown in Fig. 5 results are summarized in Table 3.

Figure 4. Significant wave height, \(H_s\) during the observational period.
Table 3: Comparison on the directional and non-directional wave parameters obtained with the DWSD and the ADCP

<table>
<thead>
<tr>
<th>Parameter</th>
<th>DWSD</th>
<th>ADCP</th>
</tr>
</thead>
<tbody>
<tr>
<td>$H_s$ (m)</td>
<td>0.03</td>
<td>-0.02</td>
</tr>
<tr>
<td>$T_a$ (s)</td>
<td>0.3</td>
<td>3.7</td>
</tr>
<tr>
<td>$T_p$ (s)</td>
<td>0.2</td>
<td>0.7</td>
</tr>
<tr>
<td>$D_p$ (°)</td>
<td>9.9</td>
<td>3.7</td>
</tr>
</tbody>
</table>

Figure 5. Scatterplots of the directional wave parameters. a) Significant wave height, $H_s$ b) Mean wave period, $T_a$ c) Peak wave period, $T_p$ and d) Peak wave direction, $D_p$.

FUTURE PERSPECTIVES AND CONCLUSIONS
The DWSD has been designed by the LDL of SIO with the objective to implement a global network of drifting wave sensors to provide a real-time data stream of directional wave parameters in support of global and regional wave forecasting, calibration and validation of scatterometer satellites, and ocean physics studies. Despite the short duration of the experiment, the positive comparison between directional and non-directional wave parameters from the DWSD and the ADCP indicates that for wind waves the bias and RMSE of the main wave parameters are well within the acceptable range for most coastal engineering applications. Possible reasons of the observed discrepancies include differences in the way the wave parameters are computed and the separation of the two sensors, that, although small, can lead to different wave forms in a very shallow water environment. More comprehensive tests are underway, which include a three-month long comparison of the DWSD performance against an accelerometric directional Datawell wavewaver deployed at a short distance from each other or mounted directly on its hard-top.

The reliability of the DWSD, its versatility and low costs can support a large number of applications. For instance, it can be considered as a useful tool for the monitoring sea conditions and waterway navigation in harbors and for planning coastal or offshore operations. The instrument could also be
suitable for meteorological and climatological studies as well as for the calibration and validation of numerical models in coastal areas. The DWSD can be useful for short-term coastal applications in developing countries, but also for well-established long-term semi-offshore (100 m depth) networks, such as the Italian Wave Recording Network (RON) set up in 1989, which is presently out of service for lack of funding. Italy has a remarkable history of coastal wave measurements and the first worldwide wave measuring station was established in the port of Genoa in 1930. A detailed inventory and wave climatology from the RON are described in the Italian Wave Atlas (Franco et al. 2004).

A second DWSD, moored in water depth of 35 m, 100 m offshore of a full-scale prototype Wave Energy Converters (WECs) termed OBREC (Overtopping BReakwater for Energy Conversion, Fig. 6) (Vicinanza et al. 2013; Vicinanza et al. 2014; Contestabile et al., 2015; Contestabile et al., 2016; Contestabile et al., 2017a; Contestabile et al., 2017b; Contestabile et al., 2017c), is under evaluation.

![OBREC prototype after his construction (a) and during a wave storm in January 2016 with filled reservoirs (b)](image)

The OBREC is designed to harvest the energy of the overtopping of the incoming waves to generate electrical power and represents the world’s first prototype of an “hybrid” WEC and can be integrated
into an existing coastal defense structure. The OBREC, whose geometry stems from recent works on the Sea Slot-cone Generator (SSG) wave energy converter (Buccino et al., 2015a; Buccino et al., 2015b), features a frontal planar ramp to facilitate the filling of a reservoir with a water level higher than the still sea level. The potential energy of the water in the reservoir is then converted into electric power with low-head turbines coupled with electrical generators located in a machine room situated beside the reservoir. The full-scale prototype is instrumented to measure its overall structural, hydraulic, power generation performance and environmental risks (Azzellino et al., 2013).

The wave observations from the two DSWD currently installed in the Gulf of Naples will be also used to validate the wave forecasting of the area as well as to calibrate and validate the numerical models for a more accurate assessment of the climatological wave energy available at the OBREC site.

ACKNOWLEDGMENTS

The development of the DWSD is supported by the NOAA grant # NA10OAR4320156 “The Global Drifter Program”. This work was also supported by the Italian Ministry of Education, University and Research (MIUR) trough the following projects:

- National Operational Programme for "Research and Competitiveness" 2007–2013 (NOP for R&C) founded project PON04a3_00303 titled “DIMEMO-Diga Marittima per l’Energia del Moto Ondoso” (Maritime Breakwater for Wave Energy Conversion), Project PON04a3_00303.
- EMSO-MedIT Strengthening of multidisciplinary marine research infrastructure in Sicily, Campania and Puglia, ESFRI EMSO, project PAC01_00044.

Partial support for LC was also provided by the University of Campania “Luigi Vanvitelli” trough the Visiting Professors scholarship 2016.

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