# CHAPTER 172

## A NEW TYPE OF BREAKWATER UTILIZING AIR COMPRESSIBILITY

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## ABSTRACT

This paper is to investigate both theoretically and experimentally the wave energy dissipation and air-pressure variation of a new type of breakwater having a pressurized air-chamber and two buoyancy tanks. The theoretical models are developed in this paper and they are shown to be in good agreement with experimental values. The new type of breakwater proposed in this paper is pointed out to attenuate the transmitted wave much better than the rectangular-shaped and concave-shaped breakwaters without the air-chamber.

# 1. INTRODUCTION

Development of a new type of breakwater having a high sea water exchange and wave energy dissipation is strongly required from environmental and disaster prevention viewpoints. This paper deals with a new type of fixed breakwater which

This paper deals with a new type of fixed breakwater which has one pressurized air-chamber and two buoyancy tanks. The great merit of the breakwater lies in the function that the resonant period can be easily adjusted only by changing the air pressure in the air-chamber without changing the geometrical shape of breakwater itself.

So far, Kiyokawa and Ohyama (1986) and Iwata et al. (1987) have discussed the wave attenuation of the breakwater with a pressurized air-chamber. There still remain, however, problems to be solved from theories and experiments.

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First of all, two theoretical models based on the Dividing Region and Source Distribution Function Methods are newly developed, which take account of air compressibility in the air-chamber. Secondary, laboratory experiments are performed not only to examine the validity of the proposed theoretical models, but also to reveal the characteristics of wave energy dissipation and variation of air pressure in the air-chamber.

### 2. THEORETICAL MODELS

The Dividing Region Method and Source Distribution Function Method are employed to evaluate changes of wave and air pressure in the air-chamber. The wave treated here is a twodimensional and irrotational small amplitude one. The fluid is assumed to be inviscid.

## 2-1. Dividing Region Method

The fluid domain is divided into five regions, as shown in Fig.l. The region I includes the incident and reflected waves and evanescent mode waves, and the transmitted wave exists in the region, V. The air pressure head R in the region III changes with wave motion. Extending the analytical treatment proposed by Iwata et al. (1986), velocity potentials in the five regions are expressed by the following:

$$\varphi_{1} = (A_{0}e^{ik(x-\ell_{2})} + B_{0}e^{-ik(x-\ell_{2})}) \frac{\cosh k(h+z)}{\cosh kh} \\ + \frac{\infty}{2} B_{n}e^{-k_{n}(x-\ell_{2})} \frac{\cos k_{n}(h+z)}{\cos k_{n}h} --- (1)$$

$$\varphi_{2} = C_{0}x + D_{0} + \frac{\infty}{2} (C_{s}\sinh\frac{s\pi x}{(1-q_{1})} + H_{s}\cosh\frac{s\pi x}{(1-q_{1})})\cos(\frac{s\pi(h+z)}{(1-q_{2})h})$$

$$----- (2)$$

$$\varphi_{3} = (E_{o}e^{ik'x} + F_{o}e^{-ik'x})(\frac{\cosh k'(h+z)}{\cosh k'h})$$

$$+ \sum_{m=1}^{\infty} (E_{m}e^{k'_{m}x} + F_{m}e^{-k'_{m}x})(\frac{\cos k'_{m}(h+z)}{\cos k'_{m}h}) + \frac{iP_{o}}{\rho\sigma}$$

$$------ (.3)$$



Fig.1 Shematic illustration of new type of breakawter with pressurized air-chamber and two buoyancy tanks and illustration, of symboles

Here,  $\emptyset_1, \emptyset_2, \emptyset_3, \emptyset_4$  and  $\emptyset_5$  are, respectively, the velocity potentials in the regions, I, II, III, IV and V, Ao the complex amplitude of incident wave (=igH\_1/2\sigma); g the gravitational acceleration, H<sub>I</sub> the incident wave height; i imaginary unit number;  $\sigma$  the angular frequency (=2 $\pi$ /T); T the wave period, B<sub>o</sub> the complex amplitude of reflected wave; I<sub>o</sub> the complex amplitude of transmitted wave; B<sub>n</sub>, C<sub>s</sub>, D<sub>s</sub>, E<sub>m</sub>, F<sub>m</sub>, G<sub>s</sub>, H<sub>s</sub> and I<sub>n</sub> (n=1, 2, 3, --, s=m=0, 1, 2, --) complex unknown coefficients; h the still water depth; x the horizontal axis; z the vertical axis; k, k<sub>n</sub>, k' and k'<sub>m</sub> the wave numbers satisfying the relationship of  $\sigma^2/g$  k tanh kh = -k<sub>n</sub> tan k<sub>n</sub> = k' tanh k'(1-q\_2)h = -k'mx tan k'm(1-q\_2)h;  $\rho$  the density of water; Po the air pressure amplitude in the air-chamber ;  $2\ell_2$  the length of air-chamber,  $2\ell_2$  the length of breakwater.

(b) Air pressure amplitude Po

The 5th term,  $iPo/p\sigma$  in Eq.(3) is the pressure term added by compressibility of air in the air-chamber. In deducing Eq.(3), the air pressure,  $P_a$  in the air-chamber is expressed as \_\_\_\_\_\_igt \_\_\_

$$P_a = \overline{Po} + Poe^{10t}$$
, ( $\overline{Po=pgq_2h} + P_{air}$ ) ----- (6)  
where,  $\overline{Po}$  is the initial air pressure and  $P_{air}$  the atomospher-  
ic pressure. The linearized dynamic boundary condition on the  
free surface in the air-chamber is

$$\eta = -i\frac{\sigma}{g}\phi_3 - \frac{P_a}{\rho g} \qquad (7)$$

where, n is the free surface elevation from the still water level.

Substitution of Eqs.(3) and (6) into Eq.(7) and assumption of uniform rise and fall of water surface in the air-chamber yield

The volume of air, V in the air-chamber is given by

.

$$V = V_0 - \eta_0 e^{10t}$$
,  $V_0 = d_0 + q_2 h$  ----- (9)

where, Vo is the initial volume of air in the air-chamber and  $d_O$  the clearance of the upper plate from the still water level at the region, I and V (see Fig.1).

Assuming the adiabatical change of air in the air-chamber, the air pressure  $P_a$  corresponding to air volume of V is given by

$$P_a = \overline{P}_0(V_0/V)^r$$
, (r = 1.4) ------ (10)

Linearization after substitution of Eqs.(6) and (9) into Eq.(10) yields

$$Po = r \overline{P}o(\eta_0 / do + q_2 h))$$
 ------ (11)

(c) Matching condition

The continuity of pressure,P and horizontal particle velocity,u is employed as the matching condition at the boundary between two regions (i.e.,  $x = \ell_1$ ,  $\ell_2$ ,  $-\ell_1$  and  $-\ell_2$ ). The pressure,  $P_j$ , (j=1 - 5) and horizontal velocity of water particle,  $u_j$ , (j=1 - 5) are estimated with

$$\begin{array}{l} P_{j}(x,z;t) = -\rho g z - i \rho \sigma \phi_{j}(x,z) e^{i \sigma t} \\ u_{j}(x,z;t) = \frac{\partial}{\partial x} (\phi_{j}) e^{i \sigma t} \end{array} \right\} \quad ----- \quad (12)$$

where, subsuffix j indicates the region, j.

(i) $x = \ell_2$	$P_{1}(\ell_{2},z;t) = P_{2}(\ell_{2},z;t)$ $u_{1}(\ell_{2},z;t) = 0$ $= u_{2}(\ell_{2},z;t)$	; $(-h \le z \le -q_1h)$ ; $(-q_1h < z \le 0)$ ; $(-h \le z \le -q_1h)$
(ii)x =- 2 <sub>2</sub>	$P_{5}(-\ell_{2},z;t)=P_{4}(-\ell_{2},z;t)$ $u_{5}(-\ell_{2},z;t)=0$ $=u_{4}(-\ell_{2},z;t)$	; $(-h \le z \le -q_1h)$ ; $(-q_1h < z \le 0)$ ; $(-h \le z \le -q_1h)$
(iii)x= L <sub>1</sub>	$\begin{array}{lll} P_{3}(\ell_{1},z;t) &= P_{2}(\ell_{1},z;t) \\ u_{3}(\ell_{1},z;t) &= 0 \\ &= u_{4}(\ell_{1},z;t) \end{array}$	; $(-h \le z \le -q_1h)$ ; $(-q_1h < z \le -q_2h)$ ; $(-h \le z \le -q_1h)$
$(iv)x = -\ell_1$	$\begin{array}{l} P_{3}(-\ell_{1},z;t) = P_{2}(-\ell_{1},z;t) \\ u_{3}(-\ell_{1},z;t) = 0 \\ = u_{4}(-\ell_{1},z;t) \end{array}$	; $(-h \le z \le -q_1h)$ ; $(-q_1h \le z \le -q_2h)$ ; $(-h \le z \le -q_1h)$
·		( 13 )

Since Ao is given as  $igH_I/2\sigma$  (known value), the unknowns of  $B_n, C_S, D_S, E_m, F_m, G_S, H_S$  and  $I_S$  (n=s=m=0,1,2,3,---) are determined by solving  $E_q.(13)$  with help of Eqs.(1) through (12). The reflection coefficient,  $r_R$  and transmission coefficient,  $r_T$  are defined by |Bo/Ao| and |Io/Ao|, respectively.

2-2. Sourse Distribution Function Method

The velocity potential in the fluid,  $\phi(x,z)$  is expressed by the sum of the incident wave velocity potential, $\phi_I$  and the scattered wave one, $\phi_D$  and  $\phi_D$  is given by a function of the Green function,G and the source distirbution function,f as follows (Nakamura et al.(1982));

$$\begin{split} \varphi(\mathbf{x}, z) &= \varphi_{I}(\mathbf{x}, z) + \varphi_{D}(\mathbf{x}, z) \\ \varphi_{D} &= \int_{S}^{f} (\mathbf{X}, Z) \cdot G(\mathbf{x}, z; \mathbf{X}, Z) ds(\mathbf{X}, Z) \\ G &= \frac{(ik^{2}-ko^{2})e^{ik} |\mathbf{x}-\mathbf{X}|}{k(hk^{2}-hko^{2}+ko)} cosh k(h+Z) cosh k(h+z) \\ &-i_{n=1} \frac{(kn^{2}+ko^{2})e^{-k_{n}} |\mathbf{x}-\mathbf{X}|}{k_{n}(hk_{n}^{2}+hko^{2}-ko^{2})} cos k_{n}(h+Z) cos k_{n}(h+z) \\ &- -----(14) \end{split}$$

where, ko is the wave number in deep water; k and kn the

wave number satisfying the relationship of  $\sigma^2/g$  =ko=k tanh kh =-k<sub>n</sub> tan k<sub>n</sub>h; x the horizontal axis; z the vertical axis with origin at still water level; X and Z the source point; i the imaginary unit number; h the still water depth; s the boundary having the source points.

Once f is determined, Po,  $r_R$  and  $r_T$  are easily obtained. The detalied calculation technique is referred to reference 4). In this study, the source points were distributed at the interval of  $\ensuremath{\Delta s/L=0.02}$  along the submerged breakwater surface under water and along the water surface in air-chamber, where  $\Delta s$  is the element length between adjacent two source points and L the wavelength at the depth of h.

## 3. LABORATORY EXPERIMENTS

### 3-1. Equipment and procedure

Water surface profiles

were measured with three

In the experiments, two wave tanks were used. Main parts of experiments were performed in an indoor wave tank in 0.9m height, 0.7m width and 25m length at Nagoya University. A flap-type wave generator controlled by Oil-pressure servo was installed at one end of the tank. The water is perfectly shut out from the area behind the wave board. Therefore, the input electrical signal is smoothly converted to the wave motion. At the other end of wave tank, a wave absorbing slope constructed with crush stone and stainless steel chips was placed so as to reduce the wave reflection to a minimum. A large wave tank in 1.6m height, 1m width and 50m length of General Technical Research Laboratory at Gikenkogyo Co.Ldt. was also used to examine the scale effect of model breakwater to the air pressure variation in the air-chamber.

Two model breakwaters made of acrylic plate, as shown in Fig.2, were employed to 680 680 investigate the wave ener-556 62 144 392 gy dissipation and air pressure variation in the The other air-chamber. types of breakwater such as concave-shaped and rectangular-shaped ones were also employed in order to discuss the difference in wave attenuation among the three types The subof breakwater. merged depth, q1h and pres-s surized head, q2h adopted in this study are listed in Table 1, which also includs  $q_1$  in case of the concave-shaped and rectan-(a) Type I gular-shaped breakwaters.

Unit: mm (b) Type II

144

Fig.2 Geometrical scale of model breakwaters with pressurized air-chamber

capacitance-type wave gauges and they were all recorded on a magnetic tape. The transmitted wave was measured with the wave gauge, No.3 which was located at about one wave length distance from back side of

2330



Fig.3 Shematic illustration of experimental set up





concaved-shaped

Type I'

Table 1 Experimental condition for three types of breakwaters (pressurizedtype, concave-shaped and rectangular-shaped breakwaters)



the breakwater. The partial standing wave profiles were measured with two wave gauges, No.1 and No.2 in order to calculate the reflection coefficient,  $r_R$ . The distance,  $\Delta x$  between the two wave gauges was changed according to the wave period; that is,  $\Delta x = (9/8)L$  for T=0.5s,  $\Delta x = (7/8)L$  for T=0.6s - 0.8s and  $\Delta x = (3/8)L$  for T≥1.0s, where L is the wave length at the depth of h. The air pressure in the air-chamber was measured with a pressure gauge (Kyowa PGM-0.5) attached to the top plate in the air-chamber.

All the experimental waves generated in this study were regular ones. The wave period employed was 0.5s,0.6s,0.65s, 0.7s,0.75s,0.8s,0.9s,1.0s,1.2s,1.4s,1.6s,2.0s, and 2.4s. The wave steepness, H/L was 0.0l for  $q_1=0.488$  and 0.02 for  $q_1=0.222$ ,0.295 and 0.422 in order to avoid wave breaking. The still water depth was 60cm throughout the experiments.

Total number of experimental runs was about 300. The experimental set-up and conditions performed in the large wave tank of GTRL at Gikenkogyo Co.Ldt. are not described here, due to limitation of paper. As mentioned above, experiments in the large wave tank were carried out to check the model scale effect to the air pressure in the air-chamber. Based on Froude similarity law, dimensions of model breakwaters, water depth and wave conditions were determined so as to correspond to experiments in small wave tank at Nagoya university. The geometrical scale in the large wave tank was selected as 1.7 times larger than that in the small wave tank. The number of experimental runs in the large wave tank was about 50.

# 3-2 Data analysis

The wave reflection coefficient,  $r_R$  was calculated with two-wave-gauges method (Goda& Suzuki(1976)), using the measured wave profiles at wave gauges No.1 and No.2. The transmission coefficient,  $r_T$  was calculated using measured wave height of wave gauge, No.3. The reflection and transmission coefficients,  $r_R$  and  $r_T$  are defined by  $H_R/H_I$  and  $H_T/H_I$ , respectively, where  $H_R$ ,  $H_T$  and  $H_I$  are the reflected, transmitted and incident wave heights, respectively.

# 3-3 Results and discussion

Using Dividing Region Method (hereafter referred to as DRM) and Source Distribution Function Method (hereafter referred to as SDFM), theoretical values of wave transmission and reflection coefficients and air pressure variation in the air-chamber were evaluated to compare with experimental values. One example is shown in Fig.4, in which experimental values are also plotted for comparison. Theoretical calculations based on the two methods are in good agreement with experimental values. Difference between theoretical values estimated with DRM and those with SDFM is recognized very small in the range of  $2k_2/L \le 0.6$ , which is general feature in this study. Since DRM requires less computatioal time than



Fig.4 Comparison of theoretically estimated values between Dividing Region Method and Source Distribution Function Method.

SDFM. In addition, theoretical values of  $Po/\rho g H_I$  estimated with DRM seem to be in better agreement with experimental values, as shown in Fig.4. Therefore, hereafter, theoretical values evaluated with DRM are employed to compare theory with experiments.

Fig.5 shows changes of the transmission coefficient,rT and the reflection coefficient,rR with  $2\ell_2/L$ . It is seen that the theoretical values agree well with experimental values. The transmission coeffcient,rT increases with decreasing of  $2\ell_2/L$  and q1. rT is expected to be less than 0.25 for  $2\ell_2/L \ge 0.3$  in case of q1=0.422, q2=0.035 and  $\ell_1/\ell_2=0.82$ , as shown in Fig.5(c). On the other hand, the reflection coefficient,rR decreases with a decrease of q1 and  $2\ell_2/L$ . rR is almost equal to 1 in the range of  $2\ell_2/L \ge 0.8$ , which is independent of q1, q2, do and  $\ell_2/\ell_1$ , as shown in Fig.4, in this study.

The effect of initial air pressure,  $\overline{P}o$  to  $r_R$  and  $r_T$  is not clearly recognized. The effect of pressurized head,  $q_{2h}$  to  $r_R$ and  $r_T$  is not clear too, although  $r_T$  seems to become smaller as  $q_{2h}$  becomes larger, as shown in Fig.4. This may be due to the reason that the experimental range of the initial air pressure,  $\overline{P}o$  and the pressurized head,  $q_{2h}$  was too narrow to affect  $r_R$  and  $r_T$ . Concerning the effect of initial air pressure or pressurized head to  $r_R$  and  $r_T$ , we will discuss later from theoretical calculations with DRM.

Fig.6 shows two examples of variations of the dimensionless air pressure amplitude,  $Po/\rho gH_I$  in the air chamber. It can be pointed out, from Fig.6, that theoretical values agree well with experimental values.  $Po/\rho gH_I$  increases monotonously as  $2 \ell_2 / L$  becomes smaller. This trend is different from those of  $r_R$  and  $r_T.$   $Po/\rho gH_I$  measured in the small wave tank is quite equal to those measured in the large wave tank. Then, the model scale effect to  $Po/\rho gH$  is not recognized in the two laboratory experiments.



Fig.5 Comparison between theoretical values and experimental values of  $r_{\rm R}$  and  $r_{\rm T}$ .



Fig.5 Comparison between theoretical values and experimental values of  $r_{\rm R}$  and  $r_{\rm T}$ .



Fig.6 Comparison between theoretical values and experimental values of  $\text{Po}/\rho\text{gH}_I$ 



Fig.7 Comparison of transmission coefficient,  $\mathbf{r}_{\rm T}$  among pressurized-type, concave-shaped and rectangular-shaped breakwaters



Fig.7 Comparison of transmission coefficient,  $r_T$  among pressurized-type, concave-shaped and rectangular-shaped breakwaters

Next, let us discuss the difference in the transmitted wave height due to the new type of breakwater (hereafter referred to as pressurized-type breakwater), and concave-shaped and rectangular-shaped breakwaters.

Figures 7(a)-(f) show experimental results of transmission coefficient,  $r_T$  due to the three different types of breakwaters. In each figure, the breakwater length,  $2l_2$  and draft depth,  $q_1h$ are quite the same among the three different types of breakwaters. It is seen that the transmission coefficient,  $r_{\rm T}$  increases largely with decreasing of  $2\ell_2/L$  in the range of  $2\ell_2/L$ ≦0.5. As shown in Figs.(a)-(f), there are no large difference in  $r_T$  due to the pressurized-type, concave-shaped and rectangular-shaped breakwaters. However, rr of the pressurized-type breakwater are comparatively smaller than those of the concaveshaped and rectangular-shaped breakwaters (see Figs.(a),(b), (e) and (f)). Therefore, it can be pointed out that the pressurized-type breakwater proposed in this study is better than the concave- and rectangular-shaped breakwaters in order to attenuate the transmitted wave.

From engineering viewpoint,  $r_T$  is frequently requested to be less than 0.5 for  $q_1{\leq}0.5$  and  $2\ell_2/L{\leq}0.4$ . As stated above, since DRM evaluates well the experimental values of  $r_T$  due to the pressurized-type breakwater, we will further discuss here, based on theoretical calculations estimated with DRM, the effect of pressurized head,  $q_2$  to  $r_T$  and geometrical dimensions of the pressurized breakwater which attenuate  $r_T$  less than 0.5 for  $q_1{\leq}0.5$  and  $2\ell_2/L{\leq}0.4$ .

Figure 8 indicates that  $r_T$  becomes smaller with increasing of the dimensionless pressurized head,  $q_2/q_1$  and  $r_T$  becomes minimal at  $q_2/q_1=1$ . Then, it can be said that increase of the pressurized head is effective to decay the transmission coefficient.

Figures 9(a)-(c) show some cases of optimum geometrical dimensions of the pressurized-type breakwater which can attenuate  $r_T$  less than 0.5 for  $q_1 {\leq} 0.5$  and  $2 \ell_2 / L {\leq} 0.5$ . It is said that  $r_T$  is also affected by  $(1 - \ell_1 / \ell_2)$  and that  $r_T$  decreases as  $(1 - \ell_1 / \ell_2)$  becomes smaller. From Fig.9, combinations of  $(1 - \ell_1 / \ell_2)$ ,  $q_1$  and  $2 \ell_2 / L$  which attenuate  $r_T$  less than 0.5 are found out in case of  $q_1 / q_2 {=} 1.0$  for three relative water depth,

h/L=0.078,0.131 and 0.207. Figure 9(c) shows that  $r_T$  becomes 0.3 when  $q_1=0.5$ ,  $2\ell_2/L=0.28$  and  $(1-\ell_1/\ell_2)=0.01$  in case of  $q_1/q_2=1.0$  and h/L=0.207. Thus, it is possible for this type of breakwater to attenuate  $r_T$  less than 0.3 in the case of  $q_1=0.5$  and  $2\ell_2/L\leq 0.4$ .

Fig.8 Effect of pressurized head,q2 to r<sub>T</sub>





#### CONCLUSIONS 4.

Wave reflection and transmission and air pressure in the air-chamber due to a new type of breakwater which has a pressurized air-chamber and two

buoyancy tanks have been discussed from theory and laboratory experiments. The main results obtained in this study are summarized as follows:

0

0

0.2

220/L

(c)

0.1

0.3

0.4

0.5

(1) The theory using the Dividing Region Method is newly developed in order to evaluate the reflection and transmission coefficients and air pressure variation in the pressurized air-chamber. The proposed theory estimates well experimental values.

(2) Theoretical calculations show that the pressurized in the air-chamber plays an important role to attenuate the transmission coefficient, rT. The transmission coefficient becomes smaller with increasing

head in the air-chamber.

(3) The transmission coefficient of the pressurized-type breakwater is comparatively smaller than those of the concaveshaped and rectangular-shaped breakwaters.

(4) The effect of Po to the refelction and transmission coefficients becomes smaller as  $2\ell_2/(do+q_1h)$  becomes larger. (5) Since the wave transmission coefficient due to the

proposed new type of breakwater can be attenuated less than 0.35 for  $2\ell_2/L\leq 0.3$  and  $q_1\leq 0.5$ , there is high possibility that this pressurized-type breakwater will be put into practical use in the sea area where high water exchange and wave decay functions are simultaneously required.

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