CHAPTER 63

3-D HYDRAULIC MODEL OF WAVES GENERATED BY DISPLACEMENTS

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ABSTRACT

Measurements were made of the water waves generated by the horizontal motion of submerged plungers. The results obtained in a three-dimensional hydraulic model experiment, using a plunger 0.5 ft. wide and 0.25 ft. high, were compared with both the experimental results and theory for the two-dimensional case. It was found that at a given location the ratio of the elevation above the still water level (SWL) of the first wave (the largest wave of the group for the range of variables tested) to the displacement of the plunger $({\rm H}_3/\lambda)$ was found to be dependent upon the Froude Number $N_{\rm Favg}$ (based upon the average plunger speed and the water depth) and upon the fatio of the height of the plunger to the water depth (D/d). For a constant value of θ , ${\rm H}_3/\lambda$ increased with increasing $N_{\rm Favg}$ and D/d. A few additional tests were made using a plunger 2.0 ft. wide and 0.25 ft. high. The results show that ${\rm H}_3/\lambda$ depends also upon the ratio of water depth to the width of the plunger (d/W).

INTRODUCTION

The generation of waves by a tectonic displacement has been solved for the two-dimensional case by García (1972) using a numerical model (ABMAC, Arbitrary Boundary Marker And Cell). García compared the results from his

*Engineer, General Electric Company, San Jose, California **Professor of Civil Engineering, University of California, Berkeley numerical model with those obtained from a hydraulic model study of several types of boundary motions for a fairly large range of Froude numbers and found that the numerical model is quite good. It appears, however, that the largest existing digital computer in the U.S. does not have the capability to permit the use of ABMAC to solve three-dimensional problems of this type, except for the case of radial symmetry. The twodimensional case is useful as an approximation to some prototype cases. For other cases it is not. Owing to this it was decided to test the applicability of the two-dimensional numerical results in three-dimensional cases, making use of a hydraulic model.

LABORATORY ARRANGEMENTS AND PROCEDURES

The experimental arrangements are shown in Fig. 1. The experiments were conducted in a tank which was 5.5 feet wide by 16 feet long by a little less than 3 feet deep. "Steps" were placed along one side wall of the tank. They were 0.50 ft. and 2.00 ft. wide, with both of them being 0.25 ft. high containing a movable plunger. The design and operation of the mechanism used to cause the plungers in the steps to move horizontally has been described by Garcia (1972) and by Das and Wiegel (1972).

A rotating boom was constructed which pivoted about a pin connection which was located at the centerline of the step, above the front end of the plunger. Parallel wire resistance wave gages (Wiegel, 1953) were mounted on the boom to sense the disturbance of the water surface. A transducer to measure the displacement of the plunger was installed between the tank frame and the moving arm (Fig. 1). The outputs of the wave gages and the plunger displacement transducer were amplified and recorded on an 8-channel strip chart recorder. A number of tests were made to check the reproducibility of results, which was found to be excellent.

Falling weights were used to drive the plunger, with the total plunger displacement (λ) occurring during a time interval T.

Wave-absorbing material was placed along the three sides of the tank to minimize reflections.

TWO-DIMENSIONAL TESTS

A series of tests were made to be certain that the new arrangements were such that Garcia's (1972) hydraulic model studies could be reproduced. To do this a vertical training wall was placed alongside the W = 0.50 ft. wide step, extending the entire length of the tank. Thus, a twodimensional channel was formed, as in Garcia's tests. A typical example of a water surface profile is shown in Fig. 2. The agreement between measurements and predictions made using the numerical model of Garcia was found to be very good.

THREE-DIMENSIONAL TESTS

The training wall described in the previous section was removed, and the waves were permitted to radiate in an entire half plane. The ratio of the first wave crest elevation above the SWL (measured along the wall) to the equivalent measurement for the two-dimension case (H₃/H₂), as a function of the normalized distance from the plunger (x/d) is shown in Fig. 3. In this figure, λ is the total displacement of the plunger, W is the width of the plunger, τ is the time required for the displacement to occur, N_{Favg} is the Froude number (V_{avg}/ $\sqrt{\text{gd}}$), V_{avg} is the average speed of the plunger movement (λ/τ), g is the acceleration of gravity and d is the water depth in the tank. For the range of conditions tested (three values of Froude number, N_{Favg}), the first wave was the highest wave. It is evident for a source of the type tested, that H₃ is much smaller than H₂, except near the source. The averages of the data shown in Fig. 4 have been plotted on logarithmic paper in Fig. 4. It can be seen that H₃/H₂ decreases as (x/d)^{-3/5} for values for x/d > 0.7. For x/d greater than about 6, H₃/H₂ is less than 0.2.

Some data on the surface spread of the waves are given in Fig. 5. Data for two of these cases were plotted in Fig. 6. The elevations of the first crest above SWL were measured at a radius of 0.50 ft. for $0 \le \theta \le 90$ degrees. These values of H_3 were plotted versus r sin θ , and it was found that there was a nearly linear relationship between the two variables. In these tests d = 0.50 ft., and the water depth above the step was 0.25 ft. (D/d = 0.50).

A number of additional tests were made, for values of d = 4, 5, 6, 7, 8 and 9 inches. The relationship between the Froude number and H_3/λ is shown in Fig. 7. The data shown in Fig. 7 and tabulated in Table 1 were obtained along the centerline in the direction of the plunger motion. These data are for a constant average plunger speed, V_{avg} , with different water depths. The two-dimensional results obtained by Garcia (1972) for a constant water depth, at x = 5 ft., are also shown in Fig. 7 for comparison. Although the location at which the measurements were made is different, it is still interesting to note that the relationship between H_3/λ and N_{Favg} has a less steep slope than is the case for the results from the two-dimensional tests. It also can be seen from Fig. 7 that for a constant Froude number the ratio H_3/λ tends to vary only slightly with λ/d within the range of variables tested. Furthermore, the ratio H_3/λ tends to be linearly related to the Froude number for values of Froude number between 0.3 and 0.4.

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The variables affecting the ratio of the normalized crest elevation of the first wave for the 0.50 ft. wide plunger are the ratios, x/d, D/d, λ/d , the angle θ as defined in Fig. 5, and the Froude number. In order to study the relationship between H₃/ λ and D/d, the other dimensionless variables were kept constant. The Froude number was kept constant by varying the plunger speed for different water depths. The desired plunger speed was obtained by using different weights that were dropped to move the plunger. To hold x/d and λ/d constant, a set of appropriate distances along the x axis and plunger displacements were chosen. The values of these parameters are given in Table 2. The results for different values of θ are shown in Fig. 8 and tabulated in Table 3. The locations at which the measurements were made are shown in Fig. 9.

The work described above (Table 3 and Fig. 8) was extended to include additional values of θ , up to 180 degrees. The results are shown in Tables 4 and 5 and in Fig. 10. A comparison of the results given in the three tables for values of $\theta = 0$, 15, 30, 45 and 60 degrees shows that the results are closely reproducible.

The curves shown in Fig. 10 were cross-plotted in Fig. 11. For large values of D/d, no data for $\theta > 135$ degrees are shown as there was no or very little water over the step and measurements were nearly meaningless. Note that for small values of D/d the curves of H/ λ versus θ were approximately symmetrical about $\theta = 90$ degrees, but were very nonsymmetrical for large values of D/d. Examples of the wave records are given in Figs. 12 and 13. It can be seen for large values of D/d that the shape of the wave is different for $\theta = 15$ than for $\theta = 165$ degrees, etc. Thus, the phenomenon is more complicated than one might expect from an observation of Fig. 11.

With the same experimental setup that was used for the 0.50 ft. wide and 0.25 ft. deep plunger, additional tests were made using a step and plunger 2.00 ft. wide and 0.25 ft. high to obtain some information on the effect of the width of the source on the height of the crest of the leading wave. Unexpected difficulties were encountered in constructing and operating the wider step and plunger, so that insufficient data were obtained. However, enough data were obtained to be of some value in understanding the phenomenon.

The locations at which the waves were measured are shown in Fig. 14. The experimental results given in Table 6 were obtained along the centerline of the step. Comparing these data with the results obtained for the 0.50 ft. wide step (Table 2) shows that H_3 for the narrow (W = 0.50 ft.) step and plunger was about 35 percent of the value for the wide (W = 2.00 ft.) step and plunger for a value of D/d of about 0.40, and a little more than 55 percent of the value for D/d equal to 1.0 (Fig. 15), all other conditions being equal.

Fig. 16 shows that for D/d < 0.5 and d/W > 1, values of ratio H_3/λ are fairly independent of y for the narrow plunger. The first wave crests in this region, behave as if they came from a point source and are nearly independent of θ . The same tendency is apparent for the wide plunger for the smallest values of D/d for which tests were made. For large values of D/d the values of H₃/ λ become quite nonuniform with respect to a constant value of r/d for both the narrow and wide plungers. It also can be seen that the waves behave as if they were generated by a combination of a line source and a point source for the case of W = 2.00 ft. for large values of D/d.

The plots of H_3/λ versus y shown in Fig. 16 for the W = 0.50 ft. plunger were shifted to the left by a value of 1.50 ft., and replotted in Fig. 17. The values are plotted as if the edge of the W = 0.50 and the W = 2.0 ft. plunger were along the same line. It is interesting to note the similarity of the two sets of data. It is also evident that the waves for the W = 2.00 ft. plunger were always higher than the waves for the W = 0.50 ft. plunger.

CONCLUSIONS

1. For the source mechanism tested, the wave crest elevation is considerably less for the three-dimensional case than for the two-dimensional case, with $\rm H_3/H_2$ decreasing in proportion to $(x/d)^{-3/5}$ for 0.7 < x/d < 10 and W/d = 1.0.

2. For small values of D/d the values of H_3/λ are fairly uniformly distributed with respect to θ for a given value of r/d, but become very nonuniform for large values of D/d.

3. Measurements of H₃ at a given value of r/d for various values of θ from 0 to 90 degrees showed that H₃ decreased in a nearly linear manner with the r sin θ , that is with the projection of the measurement point on the y axis, at least for the narrow (W = 0.50 ft.) source.

4. Values of H_3 along the centerline of the step and plunger were substantially higher for the wide (W = 2.00 ft.) source than for the narrow (W = 0.50 ft.) source, all other conditions being held constant.

5. Whether the plunger acts like line source or point source depends on the values of W/d and r/d.

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NOTATION

- d = undisturbed water depth (except over step and plunger), feet (or inches, as specified)
- D = height of step (also plunger) above bottom of tank, feet
- H_2 = elevation of first wave crest above SWL, 2-dimensional case, ft.
- H_3 = elevation of first wave crest above SWL, 3-dimensional case, ft.

 N_{Fave} = Froude number, V_{ave}/\sqrt{gd} , dimensionless

- r = radius, measured from origin, $r^2 = x^2 + y^2$
- SWL = still water level
 - t = time, seconds
- V_{avg} = average velocity of plunger (λ/τ), feet per second
 - W = width of plunger, feet
 - x = horizontal distance along the side wall of the tank measured from the front end of the step, feet

y = horizontal distance normal to the side wall of the tank, feet

- z = vertical coordinate
- λ = total plunger displacement, feet (or inches, as specified)
- τ = total time of plunger motion, seconds
- θ = horizontal angle, measured counterclockwise from the centerline of the step, degrees

Water Depth d, inches	:	4		:	5		: :	6	~	
Displacement λ , inches	6.82	: 5.75 :	: 4.50 :	: : 6.82 :	: : 5.75 :	: 4.50 :	6.82	5.75	4.50	
$\frac{\lambda}{d}$	1.70	: 1.44 :	: : 1.13	: 1.36 :	1.15	0.90	1.14	0.96	0.75	
Wave Crest (measured) H, feet	0.066	: : 0.054 :	0.040	0.046	0.037	0.027	0.038	: : 0.039 :	: : 0.022	
<u>- H3</u>	0.12	0.112	0.107	0.082	0.076	0.072	0.067	: 0.065	0.059	
Froude Number	: : 0.44 :	0.44	0.44	0.39	0.39	0.39	0.36	0.36	0.36	
Water Depth d, inches	: :	7		:	8		9			
Displacement λ , inches	: : 6.82 :	: : 5.75 :	: : 4.50	6.82	: : 5.75 :	4.50	6.82	: : 5.75	: 4.50	
$\frac{\lambda}{d}$: : 0.98 :	: : 0.82 :	: : 0.64 :	: : 0.85	: : 0.72	• • 0.56	0.76	: : 0.64	0.50	
Wave Crest (measured) H ₃ feet	: 0.034	: : 0.027	0.020	0.027	0.023	0.015	0.024	0.020	0.015	
<u>Η</u> 3 λ	: : 0.060	: : 0.056 :	0.053	0.048	: 0.047	0.040	0.042	: : 0.043	: 0.039	
Froude Number	: 0.33	. 0.33	0.33	0.31	. 0.31	: 0.31 :	0.29	: 0.29	0.29	

TABLE 1 Elevation of First Wave Crest Above SWL, as a Function of λ/d and N_{Favg} (W = 0.50 ft., θ = 0 degrees, and x = 1.00 ft.)

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TABLE 2 Elevation of First Wave Crest Above SWL, as a Function of D/d (W = 0.50 ft., x/d = 3.0, λ/d = 0.75, N_{Favg} = 0.44, θ = 0 degrees and W/d = 2.0)

Water Depth d inches	Distance Along x Axis x , feet	Displacement of Step Motion : λ, inches	: Displacement : Velocity of : plunger V avg, : ft/sec	Weight Used To: Cause Motion : 1bs : 1bs :	Wave Crest Elevation at x H ₃ feet	: <u>H</u>] : \	D d
3	0.75	2.25	1.25	1.8	0.034	0.18	1.00
4	1.00	3.00	1.44	8.2	0.021	0.086	0.75
5	1.25	3.75	1.61	19.5	0.017	0.055	0.60
6	1,50	4.50	1.77	34.0	0.014	0.037	0.50
7	1.75	5.25	1.90	75.0	0.012	0.028	0.43
8	2,00		2.04	100.0	0.012	0.022	0.38
9	2.25	6.75	2.16	121.0	0.010	0.018	0.33



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TABLE 3

Elevation of First Wave Crest Above SWL, as a Function of D/d and 8 (W = 0.5 ft., r/d = 3.0, λ/d = 0.75 N_{Favg} = 0.44 and W/D = 2.0)

Water Depth d	Elev	vation of at r/d =	First V 3.0, H ₃	lave Cres (feet)	it.	: : : :	: : :				
inches	0°	: : 15° :	: 30° :	: 45° :	: : 60° :	: 0°	: : 15° :	: : 30° :	: : 45° :	: : 60° :	
3 :	0.034	: : 0.027 :	: : 0.025 :	: : 0.019 :	: : 0.014 :	: : 0.18	: : 0.14 :	: : 0.13 :	: : 0.099 :	: : 0.075 :	: :1.00 :
4	0.021	: : 0.019 :	: : 0.016 :	: : 0.013 :	: : 0.011 :	: : 0.086 :	: : 0.077 :	: : 0.064 :	: : 0.054 :	: : 0.042 :	: :0.75 :
5	0.017	: : 0.015 :	: : 0.013 :	: : 0.011 :	: : 0.009 :	: : 0.055 :	: : 0.049 :	: : 0.042 :	: : 0.035 :	: 0.029	: :0.60 :
6	0.014	: : 0.012 :	0.011	: : 0.009	0.008	: : 0.037 :	: : 0.033 :	: : 0.029 :	: : 0.025 :	0.021	: :0.50 :
7	0.012	0.011	0.010	0.008	0.007	0.027	: 0.025	: : 0.022 :	: : 0.018 :	0.016	: :0.43
8 :	0.012	0.010	0.009	0.008	0.006	0.022	0.020	: 0.017	: 0.015	0.013	: :0.38
9 :	0.010	0.009	0.008	0.006	0.006	0.018	0.016	0.014	0.011	0.011	: 0.33

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TABLE 4

Elevation of First Wave Crest Above SWL, as a Function of θ (0 to 180 degrees), Plunger Displacement and Water Depth (W = 0.5 ft., r/d = 3.0, λ/d = 0.75, \aleph_{Pavg} = 0.44 and W/D = 2.0)

Water Depth d	: Elevation of First Wave Ctest Above SWL, H ₃ , feet :													Displace- ment of Plunger
inches	o°	15°	30°	45°	60°	75°	90°	105°	120°	135°	150°	165°	180°	; λ ; inches
3	0.037	0.031	0.025	0.019	0.013	0.010	0.008	0.006	0.005	0.004	Y	;	:	2.25
4	0.021	0.019	0.016	0.013	0.010	0.009	0.007	0.006	0.006	0.007	0.006		;	3.00
5	0.018	0.016	0.014	0.011	0.010	0.008	0.007	0.006	0.007	0.008	0.007	0.010	;	3.75
6	0.015	0.014	0.012	0.010	0.008	0.007	0.006	0.006	0.007	0.009	0.009	0.009	0.011	4.50
7	: 0.013	0.012	: 0.011	: 0.009	0.008	0.006	0.005	0.005	0.006	0.009	0,009	0.009	0.014	5.25
8	0.012	0.010	0.009	0.008	0.007	0.006	0.005	0.005	0.007	0.009	0.010	0.011	0.013	6.00
9	0.010	0.009	: 0.008	: 0.007	0.006	0.005	0.004	0.004	0.006	: 0.009	: 0.010	0.011	0.012	6.75

TAB1	Æ	5

Normalized Elevation of First Wave Crest Above SWL, as a Function of θ (0 to 180 degrees) and D/d (N = 0.5 ft., r/d = 3.0, λ/d = 0.75, N_{Favg} = 0.44 and W/D = 2.0)

Water Depth	н ₃ /λ													
inches	0°	15°	30°	45°	60°	75°	90°	105°	120°	135°	150°	165°	180°	: "
3	0.200	0.168	0.132	0.102	0.069	0.054	0.042	0.030	: 0.024	0.023	:	:		1.00
4	0.086	0.077	0.065	0.054	0.041	0.35	0.028	0.023	0.025	0.027	0.025			0.75
5 :	0.057	. 0.050	0.045	0.036	: : 0.031	: : 0.026	: : 0.022	: 0.020	: 0.022	0.026	: 0.022	: : 0.038		0.60
6	0.041	0.037	0.032	0.028	0.022	0.019	0.017	0.016	0.018	0.024	0.024	0.025	0.030	0.50
7 :	0.031	: 0.028	: : 0.024	: 0.021	: 0.018	: : 0.014	: 0.012	: 0.011	: : 0.014	: 0.020	: 0.021	: 0.021	0.032	: 0.43
8	0.023	0.020	0.018	0.015	0.013	0.011	0.010	0.010	0.013	0.018	0.020	0.022	0.026	0.36
9	0.018	0.016	: 0.015	0.013	0.011	: 0.009	: 0.008	: 0.008	. 0.011	0.015	0.017	0.020	0.022	0.33

Table 6

Elevation of First Wave Crest Above SWL, ss a Function of D/d (W = 2.0 ft., x/d = 3.0, λ/d = 0.75, $N_{\rm Favg}$ = 0.44, θ = 0 dagrees, W/D = 8.0)

Water Depth d Inches Displacement Velocity of Plunger Motion Vavg, ft/sec. Waight uaed to cause motion lba. Wave Crest Displacement of Distance $\frac{H_3}{\lambda}$ Along × Axis, × ft. Plunger λ inches Elevation at D x, feet 0.318 3 2.25 1.25 24.0 0.059 1.00 0.75 0.75 4 1.00 3.00 1.44 53.0 0.051 0.205 0.045 0.145 0.60 5 3.75 1.61 84.0 1.25 6 1.50 4.50 1.77 110.0 0.037 0.010 0.50 0.078 7 1,90 134.0 0.034 0.43 1.75 5.25 6.00 156.0 0.031 0.062 0.38 2.04 8 2,00

Note: No measurements were made for a water dapth of 9 inches

TABLE 7

Elevation of First Wave Crest Above SWL, as a Function of (x,y) and Wstar Depth (W = 2.00 ft., x/d = 3.0 for 3" < y < 21" and r/d = 3.0 for y > 21", θ/d = 0.75, N_{Favg} = 0.44 and W/D = 8.0)

Water Depth	Elevation of First Crest Above SWL, H3, test along y Direction													
d Inchas	y = 3 inches	6	9	12	15	18	21	xSin15°	²¹⁺ ^{×Sin 30°}	²¹⁺ ×Sin45°	xSin60°	21+ xSin75°	inchas	
3	. 060	.060	.060	.056	.053	.049	.042	.035	. 028	.022	.018	.013	9	
4	.056	.056	.056	.051	.047	.043	.037	.029	.023	.018	.014	.010	12	
5	.050	.050	.049	.045	.042	. 038	.033	.025	.019	.016	.012	.010	15	
6	.046	.044	.042	.038	. 036	.030	.029	. 022	.017	.013	.009	.008	18	
8	.040	.038	.037	.034	.031	.027	. 024	.021	.018	.014	.010	. 009	24	

Table 8

Normalized Elevation of First Wave Creat Above SML, as a Function of θ (W = 2.0 ft., x/d = 3.0 for 3" < y < 21" and r/d = 3.0 for y > 21", λ/d = 0.75, N_{Favg} = 0.44 and W = 8.0)

Watar Depth d inches		$\frac{H_3}{\lambda}$												
	y = 3 inches	6	9	12	15	18	21	21 + Sin15°	21 + Sin30°	21 + Sin45°	21 + Sin60°	21+ Sin 75°		
3	0.322	0.322	0.322	0.300	0.285	0.260	0.223	0.186	0.150	0.118	0.099	0.068	1.00	
4	0.223	0.223	0.223	0.206	0.187	0.171	0.149	0.117	0.093	0.071	0.058	0.040	0.75	
5	0.160	0.160	0.156	0.146	0.136	0.121	0.107	0.080	0.062	0.052	0.039	0.033	0.60	
6	0.123	0.116	0.111	0.103	0.097	0.082	0.077	0.059	0.045	0.035	0.025	0.022	0.50	
8	0.080	0.077	0.074	0.069	0.062	0.056	0.048	0.041	0.035	0.029	0.020	0.017	0.36	



FIG.I EXPERIMENTAL ARRANGEMENTS



MEASURED WAVE ELEVATION ABOUT SWL

FIG. 2 MEASURED WATER SURFACE PROFILE FOR WAVE GENERATEO BY HORIZDNTAL MOTION DF SUBMERGED STEP, COMPARED WITH THEDRY, TWO-DIMENSIDNAL MDDEL, PLUNGER DISPLACEMENT = 0.42 ft., FRUDE NUMBER = 0.32, AND d/W = 1.0



FIG. 3 H₃/H₂ VERSUS x/d, FOR W=0.50 FT., d/W=1.0 (FROM LIU_AND WIEGEL, 1974)

























FIG. 10 RELATIONSHIP BETWEEN Hy/A AND D/d AS A FUNCTION OF $\theta_{\rm r}$ for r/d=3.0, λ/d =0.75, NFavg=0.44, AND W=0.50 FT.



FIG. 11 RELATION SHIP BETWEEN H_3/ λ AND θ as a function of D/d FOR r/d = 3.0, λ /d = 0.75, N_{Favg}=0.44, AND W=0.50 FT.









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FIG. 15 (H3)0.5 / (H3)2.0 VERSUS D/d FOR x/d=3.0, X/d=0.75, NForg=0.44 AND 8= 0*



